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Theoretical Analysis of the Influence of Pore Geometry on Monomolecular Cracking and Dehydrogenation of n-Butane in Brønsted-Acidic Zeolites

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Abstract

Recent experimental work has shown that variations in the confinement of n-butane at Brønsted-acid sites due to changes in zeolite framework structure strongly affect the apparent and intrinsic enthalpy and entropy of activation for cracking and dehydrogenation. Quantum chemical calculations have provided good estimates of the intrinsic enthalpies and entropies of activation extracted from experimental rate data for MFI, but extending these calculations to less confining zeolites has proven challenging, particularly for activation entropies. Herein, we report our efforts to develop a theoretical model for the cracking and dehydrogenation of n-butane occurring in a series of zeolites containing 10-membered ring channels and differing in cavity size (TON, FER, -SVR, MFI, MEL, STF and MWW). We combine a QM/MM approach to calculate intrinsic and apparent activation parameters, with thermal corrections to the apparent barriers obtained from configurational-bias Monte Carlo simulations, to account for configurational contributions due to global motions of the transition state. We obtain good agreement between theory and experiment for all activation parameters for central cracking. For terminal cracking and dehydrogenation, good agreement between theory and experiment is found only at the highest confinements. Experimental activation parameters, especially those for dehydrogenation, tend to increase with decreasing confinement. This trend is not captured by the theoretical calculations, such that deviations between theory and experiment increase as confinement decreases. We propose that because transition states for dehydrogenation are later than those for cracking, relative movements between the fragments produced in the reaction become increasingly important in the less confining zeolites.

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3 **Keywords** (5-8)
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6 zeolites, confinement, QM/MM, CBMC, chemical kinetics, apparent rate parameters,
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8 activation enthalpy, activation entropy
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1 Introduction

Brønsted-acidic zeolites are used extensively in petroleum refining to crack alkanes (C_nH_{2n+2}) into lower molecular weight alkanes and alkenes (C_mH_{2m+2} and $C_{n-m}H_{2(n-m)}$). At very low alkane conversion, the Brønsted-acid sites are mostly unoccupied and cracking, as well as dehydrogenation (which produces C_nH_{2n} and H_2) occur by a monomolecular mechanism involving a direct activation of the alkane by the zeolite proton.¹⁻⁶ The kinetics of both monomolecular processes are first-order in alkane.⁷⁻⁹ Moreover, because alkane molecules are activated directly by protons in the rate-determining step, kinetic parameters determined from the apparent rate coefficient, k_{app} , can be used to interpret the intrinsic effects of the active site environment on catalysis. Therefore, monomolecular reactions of alkanes are useful probe reactions for characterizing the influence of zeolite structure on kinetics.

In recent experimental studies, we have shown that the apparent and intrinsic first-order rate coefficients (k_{app} and k_{int}) and the apparent and intrinsic enthalpy and entropy of activation (ΔH_{app}^\ddagger and ΔS_{app}^\ddagger , ΔH_{int}^\ddagger and ΔS_{int}^\ddagger) for central and terminal cracking and for dehydrogenation of n-butane are sensitive to the extent of reactant confinement described by the entropy of n-butane adsorption at Brønsted-acid sites (ΔS_{ads-H^+}).¹⁰ To determine values of ΔH_{int}^\ddagger and ΔS_{int}^\ddagger , we employed Eqns. 1 and 2, which follow directly from the rate expression for monomolecular cracking and dehydrogenation^{10,11}:

$$(1) \quad \Delta H_{app}^\ddagger = \Delta H_{ads-H^+} + \Delta H_{int}^\ddagger$$

$$(2) \quad \Delta S_{app}^\ddagger = \Delta S_{ads-H^+} + \Delta S_{int}^\ddagger$$

In these equations, ΔH_{ads-H^+} and ΔS_{ads-H^+} are the enthalpy and entropy of adsorption of the alkane at a Brønsted-acid site and are determined using configurational-bias Monte Carlo (CBMC) simulations because experimental adsorption measurements are not possible at temperatures

corresponding to reaction conditions (> 673 K).^{10,11} Values of $\Delta H_{\text{int}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$ can be determined by subtracting values of $\Delta H_{\text{ads-H}^+}$ and $\Delta S_{\text{ads-H}^+}$ from $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$, which are extracted directly from measured rate data and are referenced to the gas phase. The relation between apparent and intrinsic activation parameters is illustrated in Figure 1.

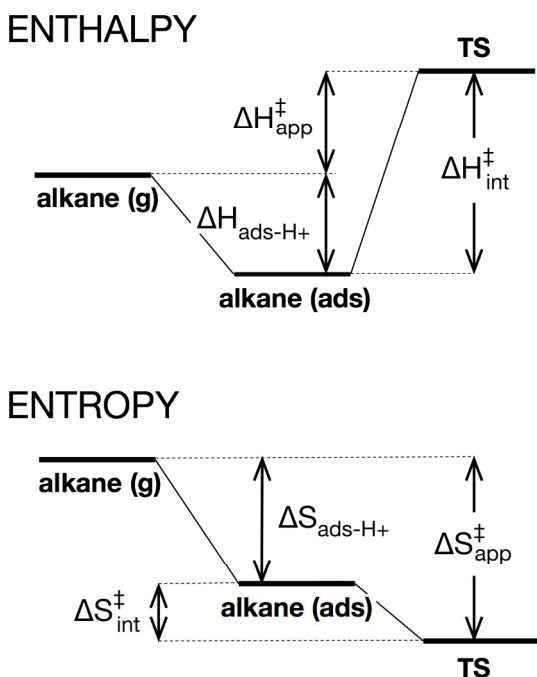


Figure 1. Schematic enthalpy and entropy landscapes for monomolecular alkane cracking or dehydrogenation over Brønsted-acid zeolites. The adsorption enthalpy ($\Delta H_{\text{ads-H}^+}$) and adsorption entropy ($\Delta S_{\text{ads-H}^+}$) of the alkane at a Brønsted-acid site is determined using configurational-bias Monte Carlo (CBMC) simulations.^{10,11} Intrinsic activation parameters ($\Delta H_{\text{int}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$) are determined by subtracting $\Delta H_{\text{ads-H}^+}$ and $\Delta S_{\text{ads-H}^+}$ from apparent parameters ($\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$) extracted directly from measured rate data.

We have found that the resulting values of $\Delta H_{\text{int}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$ depend on the zeolite framework for n-butane,¹⁰ as well as for n-hexane using previously reported rate data.¹² For n-butane, more confining zeolites (as inferred by more negative values of $\Delta S_{\text{ads-H}^+}$) exhibited lower values of $\Delta H_{\text{int}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$ for terminal cracking and for dehydrogenation, while values for central cracking are not strongly dependent on confinement.¹⁰ (For n-hexane, values of $\Delta H_{\text{int}}^{\ddagger}$

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3 and $\Delta S_{\text{int}}^{\ddagger}$ corresponded to ensemble averages over all reaction paths, as selectivity data were not
4 reported in the original study.^{10,12)} The differing dependence of activation parameters
5 corresponding to different reaction pathways on confinement was attributed to the position of
6 each transition state along its respective reaction coordinate, with $\Delta H_{\text{int}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$ for later
7 transition states (e.g., dehydrogenation) exhibiting a higher sensitivity to confinement.
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15 These findings represent the first report, to our knowledge, that the zeolite structure can
16 affect the values of $\Delta H_{\text{int}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$ because of differences in confinement. Although Gounder
17 and Iglesia¹³ have described the transition state for propane dehydrogenation as being later than
18 that of cracking based on transition-state structures obtained from density functional theory,¹⁴
19 these authors concluded that $\Delta H_{\text{int}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$ do not vary with the structural environment of
20 Brønsted-acidic protons based on arguments that a change in confinement affects the
21 stabilization of reactant and transition states to the same extent, and that a high charge density on
22 the transition state prevents confinement from affecting $\Delta S_{\text{int}}^{\ddagger}$.¹⁵ In fact, prior to our recent
23 work,¹⁰ the consensus in the literature has been that $\Delta H_{\text{int}}^{\ddagger}$ ^{12,13,16-18} and $\Delta S_{\text{int}}^{\ddagger}$ ^{12,15,16} are
24 independent of zeolite framework type and that $\Delta H_{\text{int}}^{\ddagger}$ is affected only by the “acidity” of the
25 Brønsted protons. However, these conclusions were based on experimental results for a more
26 limited number of zeolites relative to ref. 10 and on values of $\Delta H_{\text{int}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$ that were
27 estimated using Eqns. 1 and 2 together with values of $\Delta H_{\text{ads-H}^+}$ and $\Delta S_{\text{ads-H}^+}$ measured near
28 ambient temperature (which reduces the accuracy of $\Delta H_{\text{int}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$).¹¹ The recent findings of
29 ref. 10, therefore, suggest that a theoretical investigation of the effects of zeolite structure on
30 activation enthalpies and entropies for alkane monomolecular reactions is needed to better
31 understand how confinement influences these processes.
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Several theoretical studies of n-alkane monomolecular cracking and dehydrogenation have been reported previously.^{3-6,11,14,19-31} Most of these investigations have focused on determining activation energies, and good agreement between electronic structure theory and experiment was reported for a limited set of zeolites. Several studies have also reported free energies or entropies of activation.^{3,5,6,11,23,24,32} Good agreement between theory and experiment has been reported for $\Delta S_{\text{int}}^{\ddagger}$ for alkane cracking in MFI using a composite hindered rotor approach adapted from that reported by Grimme³³ to account for internal rotations.¹¹ However, no previous studies have attempted to describe the activation entropy for dehydrogenation. Positive values of $\Delta S_{\text{int}}^{\ddagger}$ for dehydrogenation have been determined experimentally,^{10,13,34} but have not been interpreted in theoretical studies.

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We also note that theoretical investigations of the effects of active site environment on kinetics have been very limited. While a few studies have investigated the effects of induced changes in acidity,^{14,24,29} only three of the abovementioned studies have investigated the effects of structural confinement.^{5,20,22} Sharada et al. have reported that activation energies for n-butane cracking and dehydrogenation differ for intersection and sinusoidal channel sites of MFI.²⁰ Bučko et al. have investigated the effect of channel environment within MOR on the intrinsic activation parameters for propane cracking using ab initio molecular dynamics simulations and transition path sampling.⁵ These authors reported that the activation entropy is less negative for 8-ring vs. 12-ring pores due to the smaller loss of entropy between the reactant and transition state in more confining locations. The same interpretation was used to explain the decrease in the experimental value of $\Delta S_{\text{int}}^{\ddagger}$ with decreasing confinement observed for n-butane central cracking in ref. 10. Maihom et al. have used density functional theory to investigate n-hexane activation within MFI and FAU.²² They showed that the intrinsic activation energy for cracking at the

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3 centermost C-C bond is nearly the same for MFI and FAU, consistent with the invariance of the
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5 experimental value of $\Delta H_{\text{int}}^{\ddagger}$ for n-butane central cracking with respect to confinement observed
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8 in ref. 10. Other reaction pathways for n-hexane cracking, such as terminal C-C cracking and
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10 dehydrogenation (those for which activation parameters were found to vary with confinement for
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12 n-butane in ref. 10), were not investigated by Maihom et al.²²
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15 The above discussion shows that a complete understanding of the influence of reactant
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17 and transition state confinement near the zeolite Brønsted-acid center on the kinetics of
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19 monomolecular alkane activation is lacking. The aim of the present study is to carry out a
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21 theoretical analysis of how the shape and size of zeolite pores affect the apparent and intrinsic
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23 enthalpies and entropies of activation for butane cracking and dehydrogenation. A previously
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25 applied QM/MM approach²⁰ is supplemented with thermal corrections, derived from CBMC
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27 simulations of n-butane adsorbed in the reactant state,¹⁰ to include configurational effects at low
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29 computational cost. Inclusion of these corrections results in good quantitative agreement between
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31 theoretically predicted and experimentally determined values of $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$ for central
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33 cracking of butane in all zeolites. Calculated values of $\Delta H_{\text{int}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$, which do not include
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35 configurational corrections, also agree well with experimentally measured values for central
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37 cracking. For terminal cracking and dehydrogenation of butane, the agreement of both apparent
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39 and intrinsic activation parameters between theory and experiment is good for zeolites with the
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41 most confining structures. As the confinement decreases, theory underestimates the experimental
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43 values of $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta H_{\text{int}}^{\ddagger}$ and (more strongly) the values of $\Delta S_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$, which increase
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45 with decreasing confinement. This deviation is much more significant for dehydrogenation than
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47 for terminal cracking and is attributed to the fact that terminal cracking and particularly
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49 dehydrogenation occur via transition states that are later than that for central cracking. The
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3 deviation of theoretical and experimental activation parameters at low confinement is very likely
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5 due to the failure of the theoretical methods to account for the non-correlated rotations and
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7 translations of the product-like fragments making up late transition state structures.
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10 11 12 13 14 **2 Theoretical Methods**

15 16 17 *2.1 Zeolite models*

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20 Seven zeolites were chosen for theoretical analysis. These zeolites (TON, FER, -SVR,
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22 MFI, MEL, STF and MWW) feature 10-ring channels and are appropriate for a study of the
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24 effects of confinement on monomolecular reaction kinetics because they represent a wide range
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26 of confinements for Brønsted-acid sites. The level of confinement for each zeolite within a given
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28 channel topology (e.g. straight vs sinusoidal channels) is described by the entropy of adsorption
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30 of n-butane adsorbed at an active site, Boltzmann averaged over all T-sites ($\Delta S_{\text{ads-H}^+}$).¹⁰ Values of
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32 $\Delta S_{\text{ads-H}^+}$ for each zeolite can be found in ref. 10.
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38 The crystallographic structures of the zeolites were taken from the database maintained
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40 by the International Zeolite Association (IZA),³⁵ and a single Al atom was introduced into each
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42 framework to create the Brønsted acid site required for catalysis. Experimental studies have
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44 shown that Al atoms are distributed among crystallographically distinct T-sites and that the
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46 distribution of Al in the framework is controlled by the Si/Al ratio and the conditions used for
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48 zeolite synthesis.^{34,36} Consequently, to appropriately compare the rate parameters determined
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50 from experiments with those predicted by theory, one should Boltzmann-average the predicted
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52 values obtained for different Al sites within each zeolite. Since this approach would be very
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54 resource-intensive, QM/MM calculations for each zeolite structure were carried out for
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3 representative T-sites chosen as discussed below, to sample the widest possible range of
4 structural environments while also considering the tendency of the adsorbed alkane to locate
5 within less confining spaces (e.g. cages, if present, rather than channels) at reaction
6 temperatures.¹¹ Selection of T-sites in this way ensures that changes in confinement occur for
7 reactant and transition states (TS) in moving from zeolites with higher average confinement (i.e.,
8 lower values of $\Delta S_{\text{ads-H}^+}$) to those with lower overall confinement (i.e., higher values of $\Delta S_{\text{ads-H}^+}$).
9 A further advantage of our approach is that it allows us to focus on distinctive cavities within
10 each of the zeolite frameworks and to be more effective in elucidating the experimentally
11 observed variations in activation parameters among the different zeolites.
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25 For the QM/MM calculations, large clusters were constructed for each of the zeolites to
26 represent the active site and the salient features of its surroundings. These clusters, along with
27 the number of tetrahedral atoms (T-atoms) included in each, are shown in Figure 2. Visual
28 representations of the pore and channel topologies of these zeolites, generated using the
29 ZEOMICS web tool,³⁷ can be found in ref. 10.
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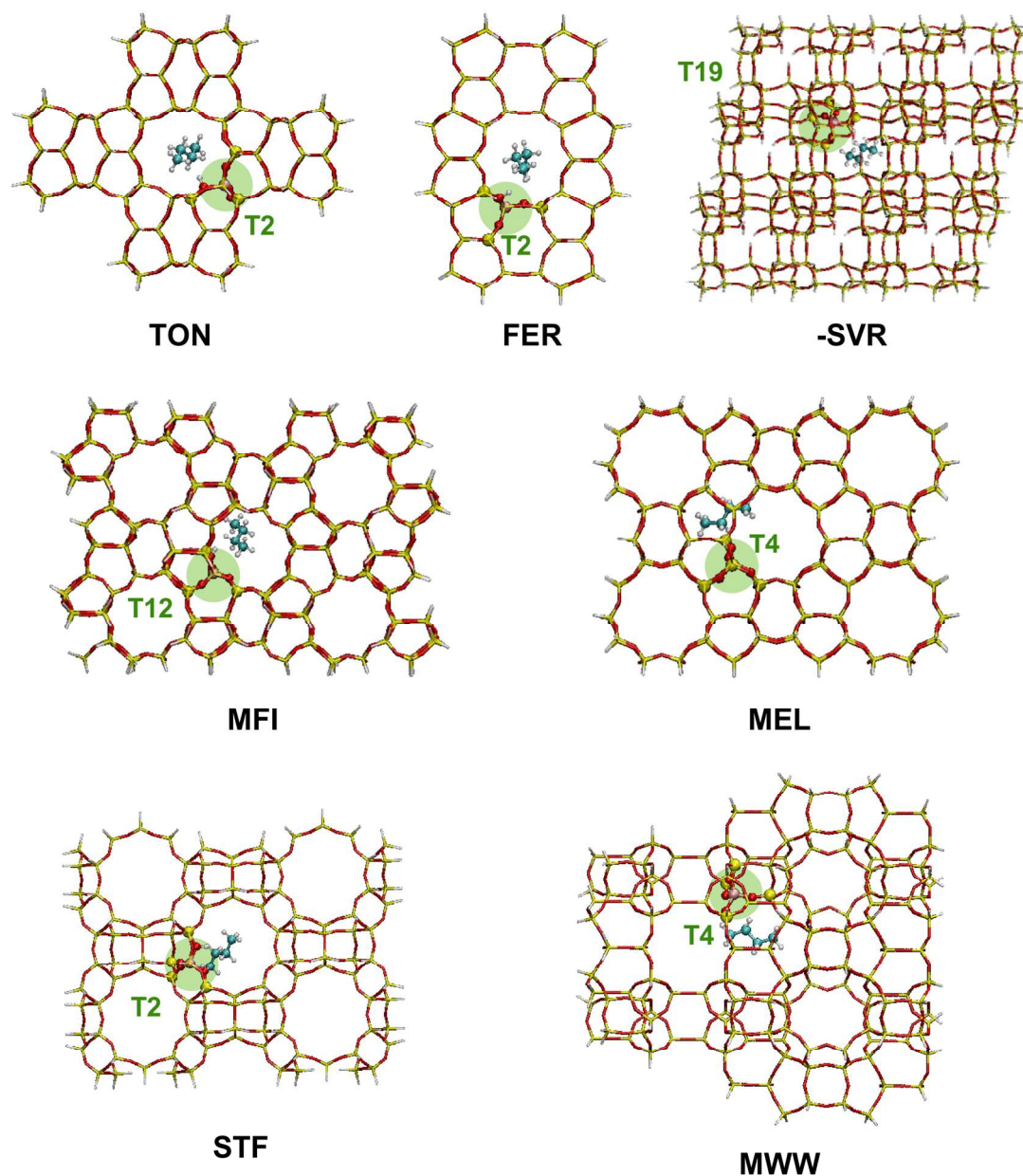


Figure 2. Cluster models used to represent the zeolite catalysts in QM/MM calculations: **TON** (280 T-atom cluster, Al in the T2 site); **FER** (236 T-atom cluster, Al in the T2 site); **-SVR** (348 T-atom cluster, Al in the T19 site); **MFI** (437 T-atom cluster, Al in the T12 site); **MEL** (264 T-atom cluster, Al in the T4 site); **STF** (398 T-atom cluster, Al in the T2 site); **MWW** (292 T-atom cluster, Al in the T4 site). The QM region is depicted using a ball-and-stick representation. Si atoms are shown in yellow, O in red, Al in pink, C in cyan and H in white.

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3 The cluster representations of the seven zeolites presented in Figure 2 can be divided into
4 three groups. The first group comprises three frameworks with straight or sinusoidal channels
5 and no cages, TON, FER and -SVR. In TON, which contains one-dimensional 10-ring straight
6 channels and 4 distinct T-sites, the Al atom was located at the T2 site, based on siting
7 probabilities estimated in a combined NMR and QM/MM study.³⁸ The -SVR framework has a
8 three-dimensional channel system, consisting of 10-ring sinusoidal channels and smaller side
9 pockets, and contains four ordered defects per unit cell, owing to Si vacancies that occur during
10 synthesis.³⁹ All terminal oxygen species surrounding these vacancies were replaced with silanol
11 groups⁴⁰ and the Al atom was placed in the T19 position, such that the Brønsted-acidic proton is
12 located in the sinusoidal channel.
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28 The second group comprises two three-dimensional frameworks featuring intersecting
29 channel systems, MFI and MEL. These structures lack large cavities, but do possess channel
30 intersections that (for MFI) are thermodynamically preferred over channel sites for n-butane
31 adsorption at 773 K.¹¹ Therefore, in MFI the Al was placed in the T12 position, which results in
32 the Brønsted-acidic proton being located at the intersection of the straight and sinusoidal
33 channels. This location offers the most available space to accommodate guest molecules and has
34 been selected in several previous studies.^{19,20,41-44} The MEL framework consists of intersecting
35 straight channels that have diameters similar to those of the MFI straight channels, but that form
36 a slightly larger cavity at their intersection.^{37,45} The Al atom in MEL was placed in the T4
37 position, such that the Brønsted-acidic proton is again situated at the channel intersection.
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53 The third group of zeolites includes two frameworks featuring large cages (> 8 Å
54 diameter based on the largest included sphere),³⁷ STF and MWW. STF consists of one-
55 dimensional 10-ring portals connecting large 18-ring pores that form the cages.⁴⁶ The Al was
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3 placed in the T2 position, to create an active site within the cage. MWW consists of two
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5 independent pore networks, one made up of 10-ring sinusoidal channels, and the other of 12-ring
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7 super cages connected by 10-ring channels.⁴⁷ Out of 8 possible distinct T sites, Al was
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9 substituted into the T4 position based on the results of computational studies that determined that
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11 this site is the most energetically stable one for Al substitution.^{48,49} This active site is also
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13 accessible from the super cage, which represents the least confining space within MWW.
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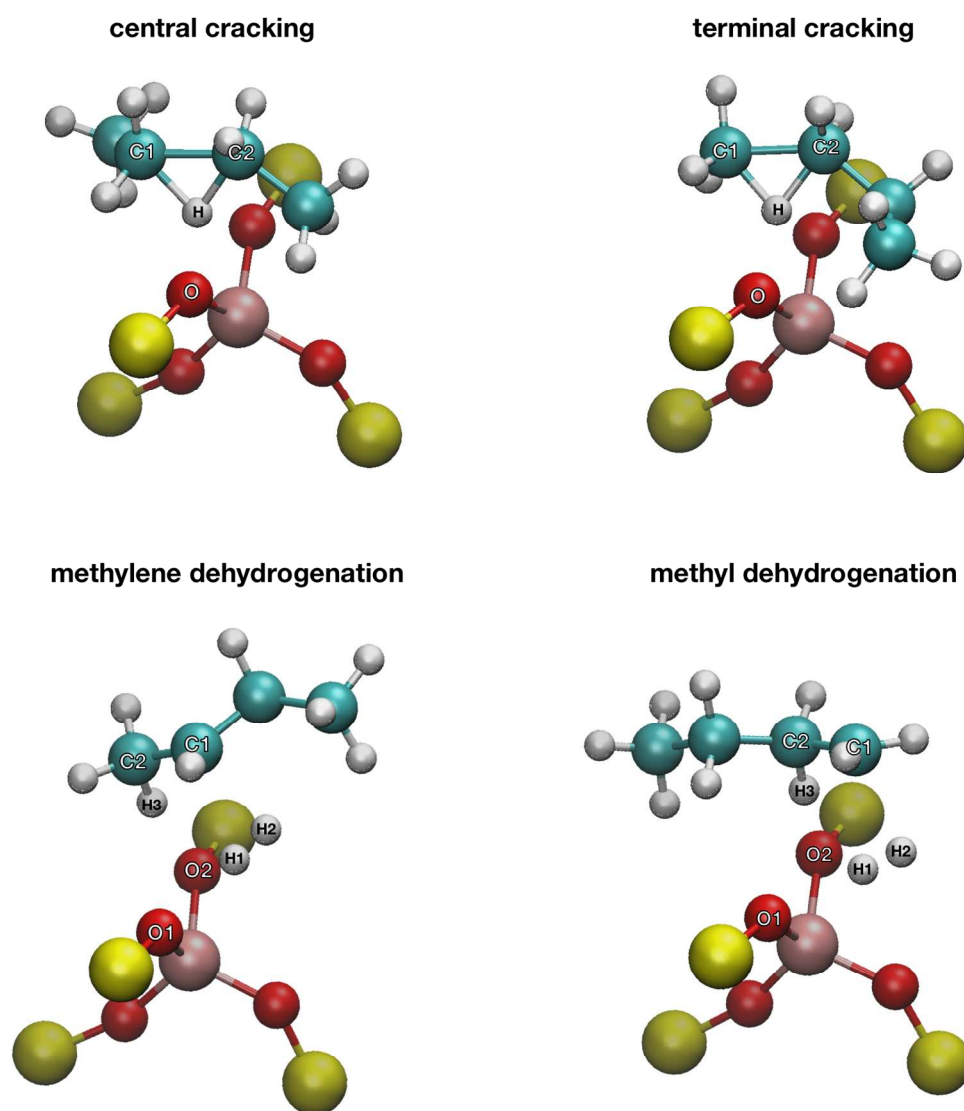
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19 As noted above, placement of Al within the largest spaces of zeolites with intersecting
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21 channels or connecting cages is supported by theoretical studies of alkane adsorption. Ab initio
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23 molecular dynamics⁵⁰ and CBMC adsorption studies¹¹ have demonstrated that, although
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25 adsorption is favored in narrow pores at lower temperatures owing to energetically favorable
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27 dispersion interactions between the framework and adsorbate, large pores are favored
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29 entropically, and therefore tend to be the preferred sites for adsorption at reaction temperatures
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31 (e.g., > 673 K). To further corroborate our placement of Al in the above specified T-sites for the
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33 QM/MM calculations in the current study, we examined the site-specific adsorption equilibrium
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35 constants ($K_{\text{ads-H}^+}$) from the CBMC simulations performed by Janda et al.¹⁰ to confirm that the
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37 formation of a reactant state for butane cracking or dehydrogenation at an active site around the
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39 selected T-sites is indeed favorable, provided Al substitution occurs there (cf. Table S1 in the
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41 Supporting Information).
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2.2 QM/MM calculations

The computational approach adopted in this study is largely similar to that used in our previous studies of alkane cracking and dehydrogenation catalyzed by MFI.^{20,34} A five tetrahedral atom (T5) cluster containing the active site and the substrate were treated quantum mechanically (QM), and the remaining framework atoms were treated using molecular mechanics (MM).^{21,51} The QM region in each of the zeolite models is highlighted using a ball-and-stick representation in Figure 2. All calculations were performed using a developmental version of Q-Chem 3.2.⁵² Initial geometries were constructed with ZEOBUILDER.⁵³ Geometry optimizations as well as vibrational analyses were carried out using the ω B97X-D functional^{54,55} and 6-311G(d,p) basis set to describe the QM region. A CHARMM-type force field was used to describe the MM region.⁵⁶⁻⁵⁸ For the zeolite Si and O atoms in the MM region, Lennard-Jones parameters and charges were taken from previous work (P2 parameter set).⁵¹ These parameters were chosen such that QM/MM adsorption energies not only match pure QM ω B97X-D/6-31+G**results, but also reproduce experimental trends in alkane adsorption energy with respect to chain length.⁵¹ For the silanol hydroxyl groups in the vacancy sites in -SVR we utilized the same MM charge parameters as for the other frameworks, adjusting the charges on the silanol groups to maintain charge neutrality of the entire cluster, rather than re-optimizing the parameters to reproduce energies calculated using pure QM on large clusters.²¹ Lennard-Jones parameters and charges for all non-zeolite atoms were taken from the CHARMM set. Single-point energy refinements on the stationary points were performed using the ω B97X-D/6-311++G(3df,3pd) level of theory for the QM region. Transition state guesses were calculated using the freezing string method (FSM)^{41,59} and optimized using the partitioned-rational function optimization (P-RFO) technique.⁶⁰

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Transition states for cracking correspond to geometries in which the Brønsted acid proton attacks the central or terminal C-C bond, since the alternative involving attack on one of the carbon atoms in the bond was found to significantly underestimate activation enthalpies, and therefore may not correspond to the true rate-limiting step for cracking.²⁰ The transition state geometries for central cracking, terminal cracking, methylene dehydrogenation and methyl dehydrogenation in MFI are shown in Figure 3. Apart from minor differences in the critical bond distances (cf., Table S2 in the Supporting Information), the transition state geometries, and therefore the mechanism for each cracking or dehydrogenation pathway remained largely invariant with the zeolite environment.



43 **Figure 3.** Transition state geometries for central cracking, terminal cracking, methylene dehydrogenation and
44 methyl dehydrogenation in MFI, with Al placed in the T12 site. For clarity, only the atoms included in the QM
45 region are shown. Si atoms are shown in yellow, O in red, Al in pink, C in cyan and H in white.

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2.3 Configurational-Bias Monte Carlo (CBMC) simulations

CBMC simulations were carried out to determine the enthalpy and entropy changes for n-butane adsorption onto Brønsted protons (i.e., in a reactant state) from the gas phase. The recently developed one-step approach using the Widom particle insertion method with domain decomposition was employed for this purpose.¹⁰ Non-bonded intra- and inter-molecular interactions are described using the 12-6 Lennard-Jones potential, and each pair-wise interaction is truncated and shifted to zero at a cut-off radius of 12.0 Å. Additionally, bonded interactions (bond stretching, bending, and torsion) are included for modeling n-butane. The potential parameters are taken from our previous work, and have been parameterized to reproduce experimentally measured heats of adsorption for linear C₃-C₆ alkanes in H-FAU.¹⁰ In all simulations, the zeolite framework was treated as a rigid structure with dimensions of at least twice the cut-off radius in all directions. At least 10 million Widom particle insertions were conducted to ensure statistically accurate results.

To better understand the adsorption configurations of n-butane in the reactant state, heat maps (i.e., probability density maps) of the locations of C atoms of butane molecules in a reactant state were generated. To obtain the C atom locations, Monte Carlo simulations in a canonical ensemble (NVT) at infinite dilution (N=1) were performed to collect n-butane configurations every 20 Monte Carlo steps. Each Monte Carlo step represents either a translational move, a rotational move, or a re-insertion move with a probability ratio of 1:1:2, respectively. A total of 4 million configurations were collected from each NVT simulation and C atom locations from more than 16,000 configurations of n-butane were used to generate the heat maps.

2.4 Calculation of enthalpies and entropies of adsorption and activation

Enthalpies and entropies of the reactant and transition states are computed from a normal mode analysis on the various stationary points identified by QM/MM calculations (cf. Section 2.2). The normal mode spectrum of an adsorbed molecule in a zeolite typically includes several low-lying frequencies that correspond to translational and rotational movements of the adsorbate relative to the zeolite framework. Previous studies have shown that treating these modes as vibrations under the rigid rotor-harmonic oscillator (RRHO) approximation typically results in overestimation of the loss in entropy associated with adsorption from the gas phase.⁶¹⁻⁶³ De Moor et al. have demonstrated that the entropy of hydrocarbons adsorbed inside zeolites cannot be treated within the RRHO approximation and that proper account must be taken of rotational and translational degrees of freedom.⁶³ These authors performed an analysis based on the Mobile Block Hessian (MBH)⁶⁴ method to identify the low-frequency modes that in reality correspond to global translations and rotations of the adsorbate, and found that replacing the corresponding vibrational contributions to the partition function by translational or rotational ones increased the configurational entropy by about 50 J mol⁻¹ K⁻¹ at 300 K.⁶³

The increases in both $\Delta S_{\text{ads-H}^+}$ and $\Delta S_{\text{int}}^\ddagger$ with decreasing confinement observed for dehydrogenation and terminal cracking of n-butane in ref. 10 suggest that the rotational and translational modes described above contribute considerably to the entropies of both reactant and transition-states. While the effects of such global motions, if similar for both states, are expected to largely cancel in calculations of $\Delta S_{\text{int}}^\ddagger$, (see Eqn. 2), contributions of such modes to $\Delta S_{\text{app}}^\ddagger$ and $\Delta S_{\text{ads-H}^+}$ are expected to be significant. Therefore, to assess the true nature of the low-frequency modes in the reactant and transition states for the cracking and dehydrogenation reactions of interest in this study, we carried out MBH calculations using the TAMKIN package.⁶⁵ This

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3 analysis (cf. Section S3 in the Supporting Information) revealed that certain low-lying vibrations
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5 in both reactant and transition states are indeed global translations and rotations of the substrate
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7 relative to the zeolite framework, indicating that applying the RRHO approximation will also
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9 affect the accuracy of apparent entropies of activation.
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14 However, while the mobile block analysis allows unambiguous identification of the
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16 vibrational modes to be replaced, the calculation of the corresponding translational entropy
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18 performed by De Moor et al. still depends upon an ad hoc estimate of the extent of the
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20 translational motion.⁶³ To avoid this issue, we instead employed a quasi-RRHO approach to
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22 mitigate some of the errors in the estimation of thermochemical quantities from vibrational
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24 frequencies.^{33,51} This method attempts to capture the thermochemical contributions from low-
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26 lying modes more accurately by a systematic interpolation between a one-dimensional free rotor
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28 at low frequencies and a harmonic oscillator at high frequencies.
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34 We have shown previously that the quasi-RRHO approach to estimate intrinsic activation
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36 enthalpies and entropies for central and terminal cracking of n-butane in MFI provides good
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38 agreement with experiments.¹¹ This approach, however, will not be sufficient for determining
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40 activation enthalpies and entropies for reactions occurring in zeolites that are less confining than
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42 MFI. The reason is that the quasi-RRHO approach relies upon a single geometry (determined
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44 using a potential energy surface at 0 K) for both the reactant and transition state, each of which at
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46 finite temperature consists of an ensemble of similar structures with slightly different
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48 orientations around the active site.^{3-5,50,66} Consequently, the entropy (and enthalpy) of the
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50 reactant and transition states will be underestimated by quasi-RRHO calculations based on single
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52 stationary points (i.e., for the reactant and transition state) with the consequence that apparent
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54 activation enthalpies and entropies will also be underestimated. On the other hand, intrinsic
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3 activation entropies will only be underestimated (or overestimated) to the extent that reactant and
4 transition states undergo differing degrees of global translation and rotation.
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9 To overcome this limitation, we derived additional thermal corrections to $\Delta H_{\text{app}}^{\ddagger}$ and
10 $\Delta S_{\text{app}}^{\ddagger}$ based on CBMC simulations (cf. Section 2.3). If the number of configurations comprising
11 the TS ensemble is assumed to be roughly similar to the number of configurations in the reactant
12 state (butane adsorbed at the Brønsted-acid site), the configurational entropy of the TS can be
13 estimated from the difference between the values of $\Delta S_{\text{ads-H}^+}$ at 773 K calculated from QM/MM
14 using the quasi-RRHO approach and those determined from CBMC simulations on butane
15 adsorption at Al in the same T-site, which naturally include contributions from global motions:
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$$(3) \quad \Delta\Delta S_{\text{config}} = \Delta S_{\text{ads-H}^+}(\text{CBMC}; 773\text{K}) - \Delta S_{\text{ads-H}^+}(\text{QM/MM-qRRHO}; 773\text{K})$$

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30 Following this procedure, the missing configurational entropy in $\Delta S_{\text{app}}^{\ddagger}$ for the different
31 reactions is estimated to be 62-86 J mol⁻¹ K⁻¹, depending on the zeolite framework (see Table 1).
32 Thermal corrections to $\Delta H_{\text{app}}^{\ddagger}$ can be determined in a similar manner. The need for such
33 corrections originates from the fact that higher-enthalpy configurations are accessible at higher
34 temperatures because of the global motions near the active site:
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$$(4) \quad \Delta\Delta H_{\text{config}} = \Delta H_{\text{ads-H}^+}(\text{CBMC}; 773\text{K}) - \Delta H_{\text{ads-H}^+}(\text{QM/MM-qRRHO}; 773\text{K})$$

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46 Values of $\Delta\Delta H_{\text{config}}$ determined using Eqn. 4 are between 10-43 kJ mol⁻¹, depending on the
47 zeolite (Table 1).
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Table 1. Thermal corrections to $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$ for each zeolite framework derived from adsorption thermodynamic data obtained using CBMC simulations at an Al atom in the T-sites used in the QM/MM calculations (in parentheses).

	$\Delta\Delta H_{\text{config}}$ kJ mol ⁻¹	$\Delta\Delta S_{\text{config}}$ J mol ⁻¹ K ⁻¹
TON (T2)	20	62
FER (T2)	10	64
-SVR (T19)	19	69
MFI (T12)	10	75
MEL (T4)	18	81
STF (T2)	11	76
MWW (T4)	43	86

The values of the entropy and enthalpy corrections are highly dependent on the specific characteristics of the zeolite (pore shape and size, location of the active site), as well as the temperature. This point is illustrated in Figure 4, which shows heat maps of the locations of C atoms for butane adsorbed in a reactant state at an Al atom in the T4 site of MWW, obtained from CBMC simulations at different temperatures. In the heat maps, the color indicates the percentage of C atom coordinates found in squares of 0.05 Å by 0.05 Å. Going from a low temperature (50 K) to the reaction temperature (773 K), the region in which butane preferentially adsorbs shifts towards the super cage and becomes significantly more diffuse. These observations demonstrate that, while the single-geometry approximation is valid at very low temperatures, this approximation breaks down at reaction temperatures (> 673 K).^{5,50} At elevated temperature, global motions contribute significantly to the enthalpy and, more strongly, to the entropy, and must be considered in calculations of the apparent enthalpies and entropies of butane cracking and dehydrogenation, as discussed below.

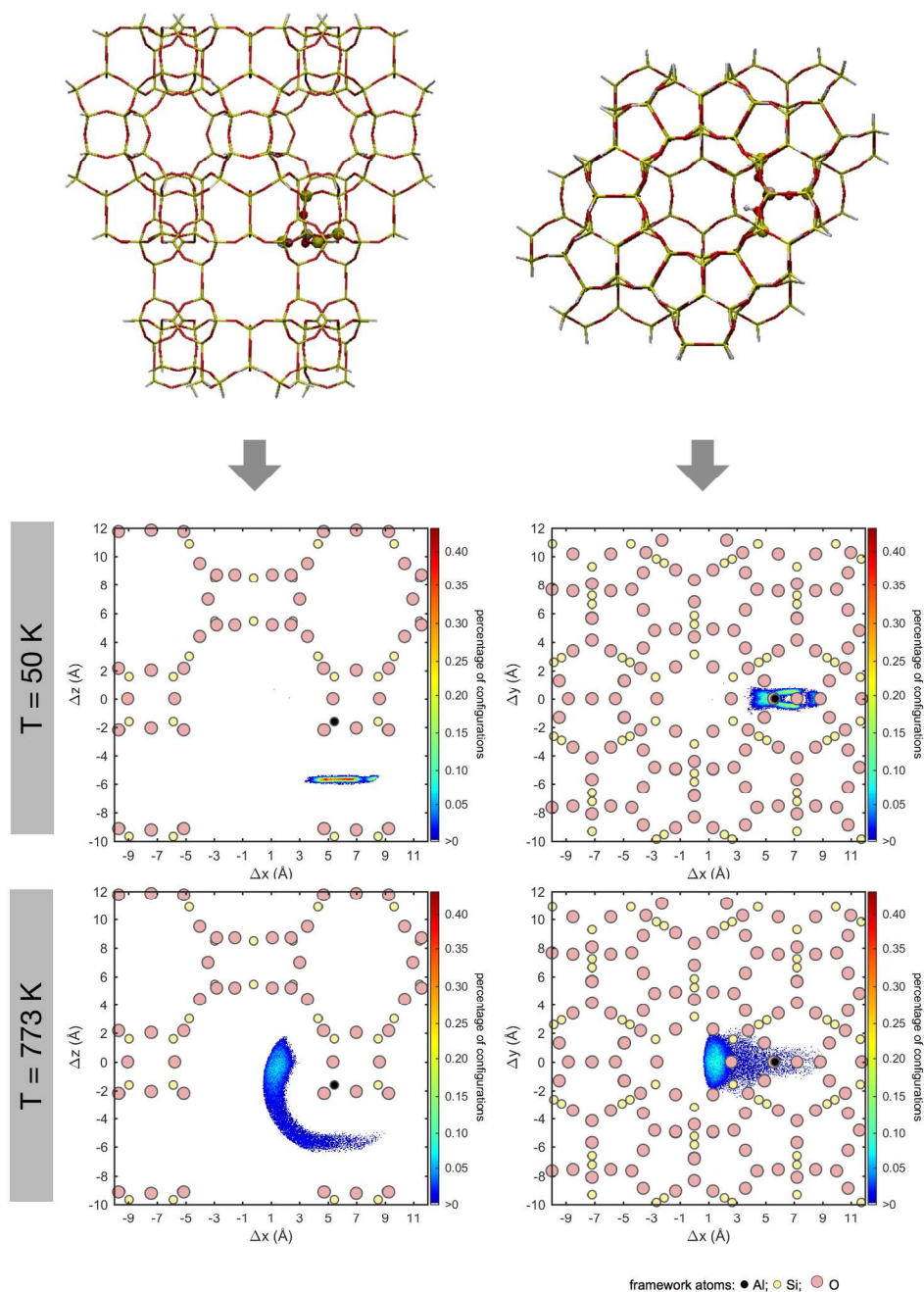


Figure 4. Heat maps showing the distribution of C atoms of the terminal C-C bond for of n-butane interacting via this bond with a Brønsted acid site at site T4 in MWW, obtained from CBMC simulations at 50 K and at 773 K. At 50 K, butane is predominantly adsorbed in the sinusoidal channel, while at 773 K, adsorption in the super cage is favored for entropic reasons. (Thumbnails of the cluster model are shown to indicate the viewing angle used to create the heat maps. Framework atoms outside the plane represented in the heat maps have been omitted for clarity.) The color scale represents the percentage of configurations in which the C atom is found in a square area of 0.05 \AA^2 .

3 Results and Discussion

3.1 Influence of the zeolite structure on activation enthalpies and entropies of *n*-butane cracking and dehydrogenation

Figures 5-8 show experimental¹⁰ as well as calculated apparent and intrinsic activation enthalpies and entropies for central cracking (Figure 5), terminal cracking (Figure 6), methylene dehydrogenation (Figure 7) and methyl dehydrogenation (Figure 8) of *n*-butane at 773 K in the zeolite frameworks of interest. In these figures, apparent parameters ($\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$) are shown in panels a and b, and their intrinsic counterparts ($\Delta H_{\text{int}}^{\ddagger}$ and $\Delta S_{\text{int}}^{\ddagger}$) are given in panels c and d. As in ref. 10, each set of activation parameters is plotted versus the Boltzmann-average values of $\Delta S_{\text{ads-H}^+}$ (calculated using CBMC simulations). The value of $\Delta S_{\text{ads-H}^+}$ serves as a proxy for the average level of confinement of *n*-butane within a given zeolite framework having a random distribution of Al atoms, with more negative values corresponding in general to more confining pore environments.¹⁰ It is important to note that confinement is a geometric concept that depends on the structural details of the framework, and could only be fully characterized by $\Delta S_{\text{ads-H}^+}$ in a perfectly homologous series of zeolites. A detailed discussion of the correlation between confinement, zeolite topology and suitable thermodynamic descriptors is given in ref. 66.

3.1.1 Central cracking

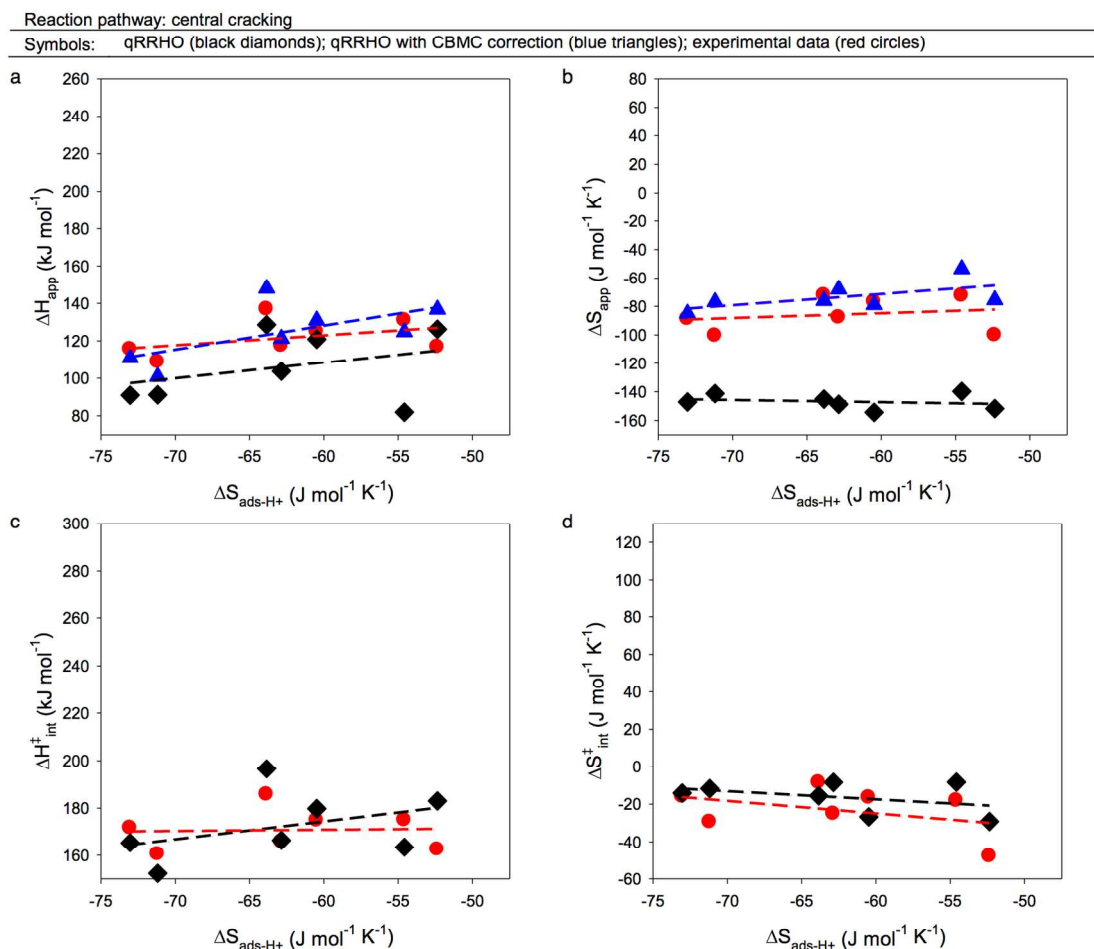


Figure 5. Plots of apparent activation enthalpy (a) and entropy (b), and intrinsic activation enthalpy (c) and entropy (d) vs. adsorption entropy determined from CBMC simulations¹⁰ for central cracking of n-butane at 773 K. Experimental values reported by Janda et al.¹⁰ (red circles) are compared with theoretical values determined from QM/MM using the quasi-RRHO approach before (black diamonds) and after (blue triangles) adding the thermal corrections derived from CBMC simulations. Representative 95% confidence intervals for the experimental values of $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$ are $\pm 7 \text{ kJ mol}^{-1}$ and $\pm 9 \text{ J mol}^{-1} \text{K}^{-1}$.¹⁰

The intrinsic and apparent enthalpies of activation for central cracking calculated using QM/MM (Figure 5, panel a and c) are in reasonably good agreement with the experimental values for all seven zeolites except $\Delta H_{\text{app}}^{\ddagger}$ for MWW. As noted in ref. 10, the uncertainty of individual experimental data points depends on the slope and the quality of the fit of the data to the Arrhenius equation. Representative 95% confidence intervals are $\pm 7 \text{ kJ mol}^{-1}$ for activation

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3 enthalpies and $\pm 9 \text{ J mol}^{-1} \text{ K}^{-1}$ for activation entropies.¹⁰ Using the quasi-RRHO approach alone,
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5 $\Delta H_{\text{app}}^{\ddagger}$ for MWW is underestimated by 49 kJ mol^{-1} . After adding $\Delta\Delta H_{\text{config}}$, however, this
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7 difference is reduced to 15 kJ mol^{-1} , bringing the data point for MWW in line with the points for
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9 the other frameworks. The agreement of theory with experiment also improves or is nearly
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11 unchanged for the remaining frameworks upon applying the CBMC corrections to $\Delta H_{\text{app}}^{\ddagger}$. The
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13 large magnitude of the correction for MWW is consistent with the large size of the super cage
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15 (which is the largest cage structure present in all zeolites investigated)¹⁰ and with the diffuse
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17 nature of the reactant-state configurations at 773 K (cf. Figure 4). The values of $\Delta H_{\text{app}}^{\ddagger}$ and
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19 $\Delta H_{\text{int}}^{\ddagger}$, determined from experiments as well as from the theoretical calculations, do not exhibit a
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21 significant correlation with $\Delta S_{\text{ads-H}^+}$. These observations are consistent with the early character of
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23 the central cracking TS,²⁰ in which the substrate is tightly bound to the active site, and is
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25 therefore expected to be relatively insensitive to the size and geometry of the zeolite cavity.
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33 Experimental and calculated apparent and intrinsic entropies of activation for central
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35 cracking are shown in panels b and d of Figure 5. While intrinsic activation entropies from
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37 theory and experiment are in reasonable agreement, apparent entropy changes calculated using
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39 the quasi-RRHO approach underestimate the experimental values by $41\text{-}77 \text{ J mol}^{-1} \text{ K}^{-1}$ depending
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41 on the framework. This discrepancy appears to result from the global motions of the transition
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43 state, which are not accounted for in the QM/MM calculations, since adding $\Delta\Delta S_{\text{config}}$ to $\Delta S_{\text{app}}^{\ddagger}$
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45 improves the agreement significantly for all zeolites, again leaving no clear trend between the
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47 remaining discrepancies and the framework type. The value of $\Delta\Delta S_{\text{config}}$ ranges from 62 to 89 J
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49 $\text{mol}^{-1} \text{ K}^{-1}$, with the lower values corresponding to the most confining zeolite topologies (TON,
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51 FER and -SVR) because as the size of the zeolite cavity increases, adsorbed alkanes have greater
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53 freedom to rotate and translate. Consequently, the configurational entropy unaccounted for by
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3 the quasi-RRHO approach is correspondingly larger. In the more confining zeolite frameworks,
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5 both the reactant and the TS are less free to translate or rotate, and therefore entropy
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7 contributions from these modes are closer in magnitude to the vibrational estimates.
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3.1.2 Terminal cracking

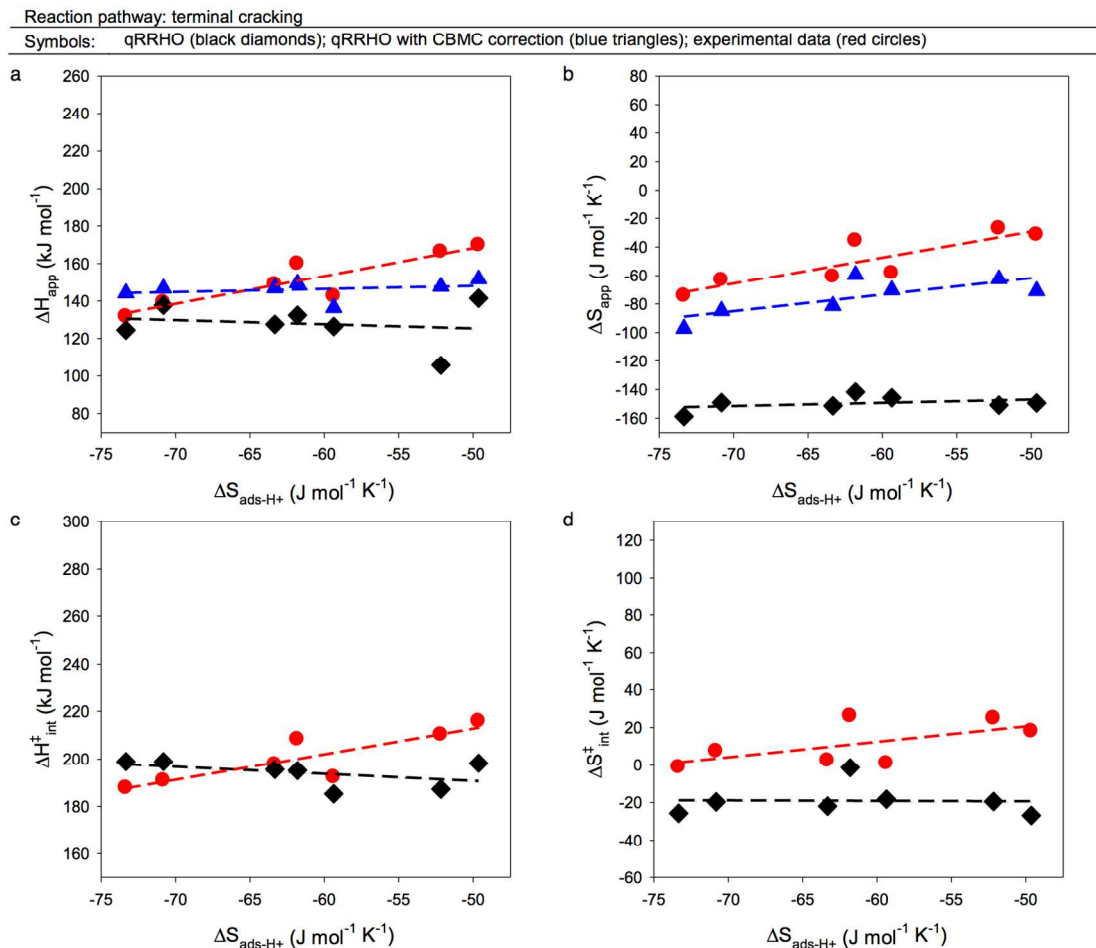


Figure 6. Plots of apparent activation enthalpy (a) and entropy (b), and intrinsic activation enthalpy (c) and entropy (d) vs. adsorption entropy determined from CBMC simulations¹⁰ for terminal cracking of n-butane at 773 K. Experimental values reported by Janda et al.¹⁰ (red circles) are compared with theoretical values determined from QM/MM using the quasi-RRHO approach, before (black diamonds) and after (blue triangles) adding the thermal corrections derived from CBMC simulations. Representative 95% confidence intervals for the experimental values of $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$ are $\pm 7 \text{ kJ mol}^{-1}$ and $\pm 9 \text{ J mol}^{-1} \text{ K}^{-1}$.¹⁰

Apparent and intrinsic enthalpies and entropies of activation for terminal cracking are shown in Figure 6. The activation enthalpies for terminal cracking are higher relative to those for central cracking (Figure 5). Calculated values of $\Delta H_{\text{int}}^{\ddagger}$ and CBMC-corrected values of $\Delta H_{\text{app}}^{\ddagger}$ are generally in good agreement with experimentally observed values, especially considering the

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3 representative uncertainty of +/- 7 kJ mol⁻¹ on the latter, although the agreement is better for the
4 more confining frameworks than for the two least confining frameworks, MWW and STF. In
5 contrast to central cracking, the experimental enthalpies and entropies of activation show a slight
6 upward trend going from more to less confining frameworks. This trend is not captured by the
7 QM/MM values without the configurational correction term, resulting in an increasing deviation
8 between theory and experiment with decreasing confinement. After adding the configurational
9 corrections derived from CBMC, an upward trend in the apparent activation parameters with
10 respect to $\Delta S_{\text{ads-H}^+}$ can be seen that is qualitatively similar to that exhibited by the experimental
11 data. This observation supports the validity of the assumption that the transition state for terminal
12 cracking possesses similar rotational and translational entropy to that of the reactant state. The
13 effect of adding the CBMC correctional terms to $\Delta H_{\text{app}}^\ddagger$ and $\Delta S_{\text{app}}^\ddagger$ is to account for such
14 motions, and the entropy contributed by these modes increases with decreasing confinement.

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33 However, despite the similar trends seen in the experimental and CBMC-corrected values
34 of $\Delta H_{\text{app}}^\ddagger$ and $\Delta S_{\text{app}}^\ddagger$, calculated values of $\Delta S_{\text{app}}^\ddagger$ and (to a lesser extent) $\Delta H_{\text{app}}^\ddagger$ are
35 systematically more negative than experimentally measured values, especially at lower
36 confinement, which suggests that an additional source of entropy becomes increasingly
37 important to the transition state at low confinement. The source of this entropy could be rotation
38 of the ethyl group adjacent to the breaking C-C bond (cf. Figure 3), resulting in a more flexible
39 TS with a larger conformational space for terminal cracking. The effect of this internal rotation is
40 expected to be more prominent in the less confining frameworks.

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3.1.3 Dehydrogenation

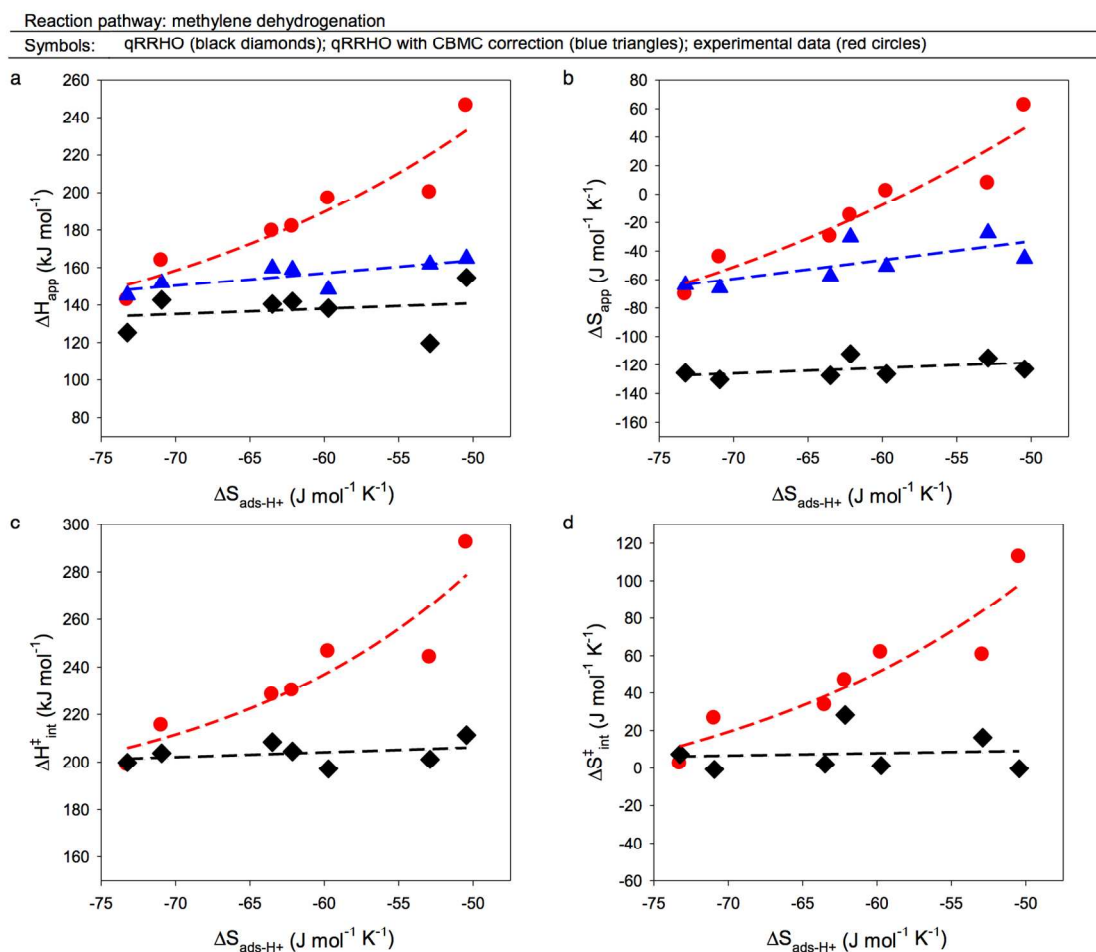


Figure 7. Plots of apparent activation enthalpy (a) and entropy (b), and intrinsic activation enthalpy (c) and entropy (d) vs. adsorption entropy determined from CBMC simulations¹⁰ for methylene dehydrogenation of n-butane at 773 K. Experimental values reported by Janda et al.¹⁰ (red circles) are compared with theoretical values determined from QM/MM using the quasi-RRHO approach, before (black diamonds) and after (blue triangles) adding the thermal corrections derived from CBMC simulations. Representative 95% confidence intervals for the experimental values of $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$ are $\pm 8 \text{ kJ mol}^{-1}$ and $\pm 11 \text{ J mol}^{-1} \text{K}^{-1}$.¹⁰

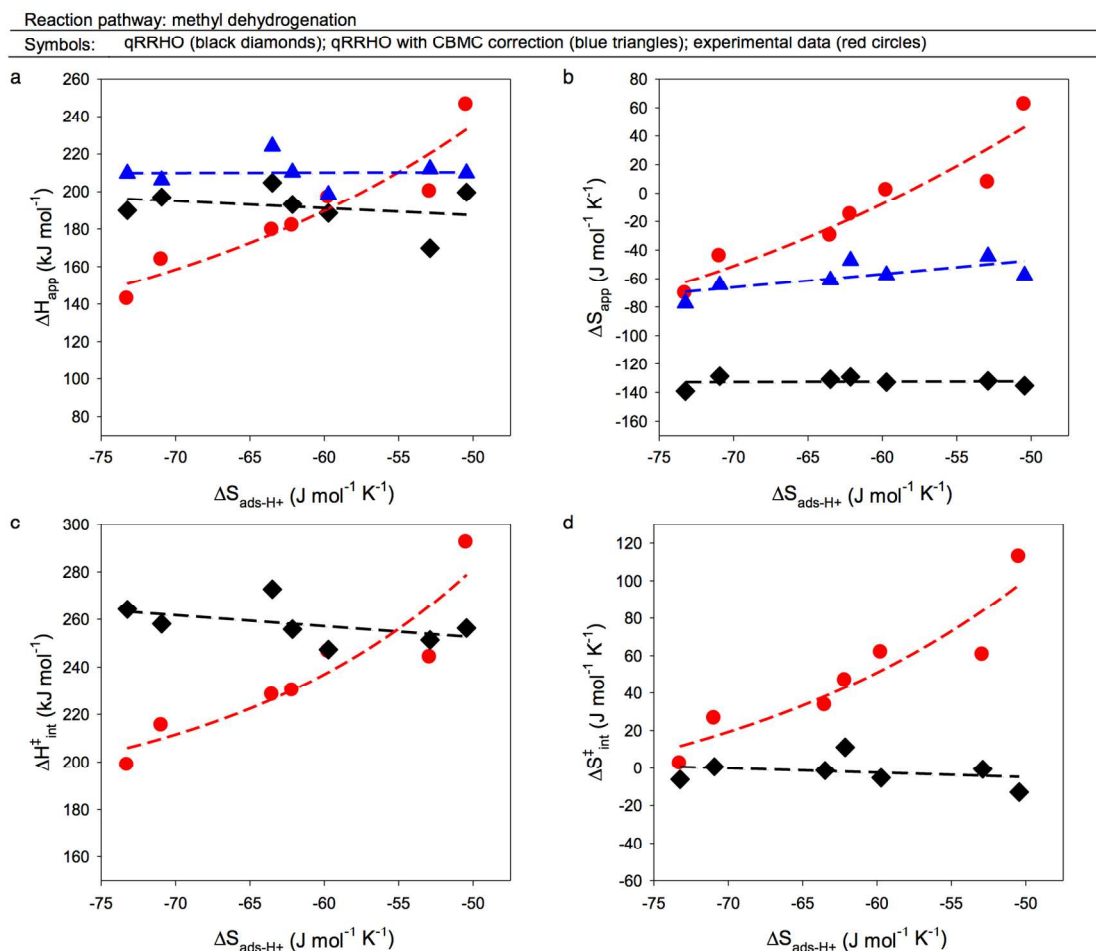


Figure 8. Plots of apparent activation enthalpy (a) and entropy (b), and intrinsic activation enthalpy (c) and entropy (d) vs. adsorption entropy determined from CBMC simulations¹⁰ for methyl dehydrogenation of n-butane at 773 K. Experimental values reported by Janda et al.¹⁰ (red circles) are compared with theoretical values determined from QM/MM using the quasi-RRHO approach, before (black diamonds) and after (blue triangles) adding the thermal corrections derived from CBMC. Representative 95% confidence intervals for the experimental values of $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$ are $\pm 8 \text{ kJ mol}^{-1}$ and $\pm 11 \text{ J mol}^{-1} \text{K}^{-1}$.

Activation parameters corresponding to n-butane dehydrogenation via activation of methylene and methyl C-H bonds are presented in Figure 7 and Figure 8, respectively. Because butene undergoes rapid 1,2 isomerization at reaction temperatures, the contribution of methylene and methyl dehydrogenation pathways to the rate cannot be determined experimentally.

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3 Therefore, computed activation parameters for both methylene dehydrogenation (Figure 7) and
4 methyl dehydrogenation (Figure 8) must be compared with experimental values to gain
5 mechanistic insights. However, the calculated values of $\Delta H_{\text{app}}^{\ddagger}$ are significantly higher for
6 methyl C-H activation (Figure 8, panel a) than for methylene C-H activation (Figure 7, panel a),
7 in line with the generally accepted stability order of the carbenium ions formed in the respective
8 transition states (methyl C-H: primary carbenium ions; methylene C-H secondary carbenium ion
9 – cf. Figure 3), while the calculated values of $\Delta S_{\text{app}}^{\ddagger}$ are similar for both pathways (panel b in
10 Figures 7 and 8). Therefore, the methylene dehydrogenation pathway is expected to prevail in all
11 frameworks, and further discussion is centered on a comparison of theory with experiment for
12 methylene dehydrogenation (Figure 7).
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28 Values of $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$ calculated using the quasi-RRHO approach (black symbols)
29 significantly underestimate the experimentally measured ones for all zeolite frameworks. For
30 dehydrogenation, the experimentally observed increase in $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$ with decreasing
31 confinement is not properly recovered by the QM/MM calculations. When the configurational
32 corrections derived from CBMC are added to the QM/MM values, better agreement is obtained
33 between experiment and theory for $\Delta H_{\text{app}}^{\ddagger}$, and especially for $\Delta S_{\text{app}}^{\ddagger}$. An upward trend emerges
34 in $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$ with respect to $\Delta S_{\text{ads-H}^+}$, albeit not as strong as that exhibited by the
35 experimental values. Consequently, as confinement decreases, the discrepancy between
36 experiment and theory increases more significantly than for terminal cracking. These deviations
37 may be attributed to the later transition state for dehydrogenation compared to cracking.²⁰ For
38 dehydrogenation, the H₂ product is virtually completely formed and is already moving away
39 from the nascent butene (cf. Figure 3). Relative movements between the two fragments of the
40 more disjointed TS remain unaccounted for by the CBMC corrections, which only reflect the
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3 global mobility of the TS about the active site as derived from calculations of reactant
4 adsorption. These relative motions become increasingly prominent in less confining frameworks,
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6 and would also affect $\Delta S_{\text{int}}^{\ddagger}$ and $\Delta H_{\text{int}}^{\ddagger}$, due to configurations of the TS with an increased charge
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8 separation. For both intrinsic parameters, an increasing deviation between theory and experiment
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10 is also observed with decreasing confinement. The magnitude of these deviations for $\Delta S_{\text{int}}^{\ddagger}$ are
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12 furthermore consistent with simplified statistical mechanics estimates of the entropy generated
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14 upon forming products of n-butane dehydrogenation within the MFI intersection.³⁴
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21 For reactions with increasingly loose transition states, especially in more open frameworks,
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23 the free energy bottlenecks separating reactants and products may be very different from the
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25 enthalpy bottlenecks identified by the saddle points optimized at 0 K.⁶⁷ Higher enthalpy
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27 configurations may become relevant due to favorable entropy, and a more rigorous description of
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29 the transition state based on molecular dynamics (MD) methods that allow sampling the
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31 complete free energy space at operational temperatures may be required. Accelerated sampling
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33 methods to simulate reactions with ab initio MD such as metadynamics,⁶⁸ combined with
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35 umbrella sampling,⁶⁹ and transition path sampling^{70,71} have recently found application in zeolite
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37 catalysis.^{3-5,50,72-78} While these powerful approaches are very promising, they come with a much
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39 higher computational cost. Furthermore, separating the obtained free energy barriers into
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41 individual enthalpy and entropy contributions is not straightforward and requires further
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43 investigation.
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4 Conclusions

We have performed a theoretical study of the effects of zeolite topology on butane cracking and dehydrogenation to elucidate the experimentally observed variations in activation enthalpy and entropy for these reactions. We have leveraged a combination of CBMC simulations with QM/MM calculations employed in previous work to account for configurational enthalpy and entropy due to the mobility of the substrate within the zeolite cavity. Following this approach, we obtained apparent and intrinsic enthalpies and entropies of activation in good agreement with experiment for central cracking. For central cracking, which has an early transition state, $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$ show no significant correlation with framework confinement. The corrections derived from CBMC successfully account for configurational enthalpy and entropy due to global motions of the transition state, resulting in good agreement of the apparent activation parameters between theory and experiment for all zeolites. For terminal cracking, experimental enthalpies and entropies of activation show an upward trend with decreasing confinement of the zeolite framework, which is not entirely captured by the calculations. Good agreement is still attained for the narrower pore topologies, but increasing deviations between theory and experiment emerge for the less confining zeolites, suggesting that an additional contribution of entropy to the transition state becomes increasingly important at low confinement. This effect is even more pronounced for dehydrogenation. While it is not possible to distinguish between methylene and methyl dehydrogenation experimentally, calculations indicate that the methylene pathway would prevail because its lower activation enthalpy is lower, and both pathways have a similar activation entropy. The experimentally observed increase in $\Delta H_{\text{app}}^{\ddagger}$ and $\Delta S_{\text{app}}^{\ddagger}$ with decreasing confinement is not fully reproduced by the calculations, even after including the corrections from CBMC. Because transition states for dehydrogenation occur later along the reaction coordinate

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3 than for cracking, increased relative movements emerge between the saturated fragment expelled
4 in the reaction (C_2H_6 in central cracking, CH_4 in terminal cracking, H_2 in dehydrogenation) and
5 the remaining alkene, in addition to the global motions accounted for by the CBMC corrections.
6 Such motions also affect ΔH_{int}^\ddagger and ΔS_{int}^\ddagger , for which an increasing deviation between theory and
7 experiment is also observed with decreasing confinement. These observations indicate that as
8 transition states become increasingly loose, they can no longer be adequately characterized by
9 single saddle points, especially in less confining zeolites, and more advanced sampling methods
10 based on ab initio molecular dynamics will be necessary to correctly identify the free energy
11 bottlenecks for these reactions.
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25 **5 Supporting Information**

26 Additional details on the accessibility assessment of the T-sites selected for Al substitution,
27 overview of critical distances in the transition states for butane cracking and dehydrogenation,
28 additional details of the Mobile Block analysis performed on the reactant and transition states
29 obtained from QM/MM.
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40 **6 Acknowledgements**

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7 References

- (1) Haag, W. O.; Dessau, R. M. *Proceedings – International Congress on Catalysis*, 8th, Berlin, Verlag Chemie: Weinheim, 1984; Vol. 2, pp 305–316.
- (2) Kotrel, S.; Knözinger, H.; Gates, B. C. *Micro. Meso. Mater.* **2000**, 35-36, 11–20.
- (3) Bučko, T.; Benco, L.; Dubay, O.; Dellago, C.; Hafner, J. *J. Chem. Phys.* **2009**, 131, 214508.
- (4) Bučko, T.; Hafner, J. *J. Phys.: Condens. Matter* **2010**, 22, 384201.
- (5) Bučko, T.; Benco, L.; Hafner, J.; Ángyán, J. G. *J. Catal.* **2011**, 279, 220–228.
- (6) Zimmerman, P. M.; Tranca, D. C.; Gomes, J.; Lambrecht, D. S.; Head-Gordon, M.; Bell, A. T. *J. Am. Chem. Soc.* **2012**, 134, 19468–19476.
- (7) Konno, H.; Okamura, T.; Kawahara, T.; Nakasaka, Y.; Tago, T.; Masuda, T. *Chem. Eng. J.* **2012**, 207-208, 490–496.
- (8) Voogd, P.; Van Bekkum, H. *Appl. Catal.* **1990**, 59, 311–331.
- (9) Haag, W. O.; Lago, R. M.; Weisz, P. B. *Faraday Discuss. Chem. Soc.* **1981**, 72, 317–330.
- (10) Janda, A.; Vlaisavljevich, B.; Lin, L.-C.; Smit, B.; Bell, A. T. *J. Am. Chem. Soc.* **2016**, 138, 4739–4756.
- (11) Janda, A.; Vlaisavljevich, B.; Lin, L.-C.; Sharada, S. M.; Smit, B.; Head-Gordon, M.; Bell, A. T. *J. Phys. Chem. C* **2015**, 119, 10427–10438.
- (12) van Bokhoven, J. A.; Williams, B. A.; Ji, W.; Koningsberger, D. C.; Kung, H. H.; Miller, J. T. *J. Catal.* **2004**, 224, 50–59.
- (13) Gounder, R.; Iglesia, E. *J. Am. Chem. Soc.* **2009**, 131, 1958–1971.
- (14) Zheng, X.; Blowers, P. *J. Phys. Chem. A* **2005**, 109, 10734–10741.
- (15) Gounder, R.; Iglesia, E. *Acc. Chem. Res.* **2012**, 45, 229–238.
- (16) Ramachandran, C. E.; Williams, B. A.; van Bokhoven, J. A. *J. Catal.* **2005**, 233, 100–108.
- (17) van Bokhoven, J. A.; Xu, B. *Stud. Surf. Sci. Catal.* **2007**.
- (18) Babitz, S. M.; Williams, B. A.; Miller, J. T.; Snurr, R. Q.; Haag, W. O.; Kung, H. H. *Appl. Catal. A Gen* **1999**, 179, 71–86.
- (19) Swisher, J. A.; Hansen, N.; Maesen, T.; Keil, F. J.; Smit, B.; Bell, A. T. *J. Phys. Chem. C* **2010**, 114, 10229–10239.
- (20) Sharada, S. M.; Zimmerman, P. M.; Bell, A. T.; Head-Gordon, M. *J. Phys. Chem. C* **2013**, 117, 12600–12611.
- (21) Zimmerman, P. M.; Head-Gordon, M.; Bell, A. T. *J. Chem. Theory Comput.* **2011**, 7, 1695–1703.
- (22) Maihom, T.; Pantu, P.; Tachakritikul, C.; Probst, M.; Limtrakul, J. *J. Phys. Chem. C* **2010**, 114, 7850–7856.
- (23) Tranca, D. C.; Hansen, N.; Swisher, J. A.; Smit, B.; Keil, F. J. *J. Phys. Chem. C* **2012**, 116, 23408–23417.
- (24) Ding, B. J.; Huang, S. P.; Wang, W. C. *Chin. J. Chem.* **2008**, 26, 1173–1180.
- (25) Zygmunt, S. A.; Curtiss, L. A.; Zapol, P.; Iton, L. E. *J. Phys. Chem. B* **2000**, 104, 1944–1949.
- (26) Frash, M. V.; van Santen, R. A. *Top. Catal.* **1999**, 9, 191–205.
- (27) Rigby, A. M.; Kramer, G. J.; van Santen, R. A. *J. Catal.* **1997**, 170, 1–10.
- (28) Kazansky, V. B.; Frash, M. V.; van Santen, R. A. *Appl. Catal. A Gen.* **1996**, 146, 225–

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- 247.
- (29) Blaszkowski, S. R.; Nascimento, M. A. C.; van Santen, R. A. *J. Phys. Chem.* **1996**, *100*, 3463–3472.
- (30) Collins, S. J.; O'Malley, P. J. *Chem. Phys. Lett.* **1995**, *246*, 555–561.
- (31) Collins, S. J.; O'Malley, P. J. *J. Catal.* **1995**, *153*, 94–99.
- (32) Bučko, T. *J. Phys.: Condens. Matter* **2008**, *20*, 064211.
- (33) Grimme, S. *Chemistry* **2012**, *18*, 9955–9964.
- (34) Janda, A.; Bell, A. T. *J. Am. Chem. Soc.* **2013**, *135*, 19193–19207.
- (35) Structure Commission of the International Zeolite Association. <http://www.iza-structure.org/databases/>.
- (36) Dědeček, J.; Sobalík, Z.; Wichterlová, B. *Catal. Rev.* **2012**, *54*, 135–223.
- (37) First, E. L.; Gounaris, C. E.; Wei, J.; Floudas, C. A. *Phys. Chem. Chem. Phys.* **2011**, *13*, 17339–17358.
- (38) Sklenak, S.; Dědeček, J.; Li, C.; Gao, F.; Jansang, B.; Boekfa, B.; Wichterlová, B.; Sauer, J. *Collect. Czech. Chem. Commun.* **2008**, *73*, 909–920.
- (39) Baerlocher, C.; Xie, D.; McCusker, L. B.; Hwang, S.-J.; Chan, I. Y.; Ong, K.; Burton, A. W.; Zones, S. I. *Nat. Mater.* **2008**, *7*, 631–635.
- (40) Bushuev, Y. G.; Sastre, G. *J. Phys. Chem. C* **2009**, *113*, 10877–10886.
- (41) Gomes, J.; Zimmerman, P. M.; Head-Gordon, M.; Bell, A. T. *J. Phys. Chem. C* **2012**, *116*, 15406–15414.
- (42) Van Speybroeck, V.; Van der Mynsbrugge, J.; Vandichel, M.; Hemelsoet, K.; Lesthaeghe, D.; Ghysels, A.; Marin, G. B.; Waroquier, M. *J. Am. Chem. Soc.* **2011**, *133*, 888–899.
- (43) Van der Mynsbrugge, J.; Hemelsoet, K.; Vandichel, M.; Waroquier, M.; Van Speybroeck, V. *J. Phys. Chem. C* **2012**, *116*, 5499–5508.
- (44) Van der Mynsbrugge, J.; Visur, M.; Olsbye, U.; Beato, P.; Bjørgen, M.; Van Speybroeck, V.; Svelle, S. *J. Catal.* **2012**, *292*, 201–212.
- (45) Kokotailo, G. T.; Chu, P.; Lawton, S. L.; Meier, W. M. *Nature* **1978**, *275*, 119–120.
- (46) Paul Wagner; Yumi Nakagawa; Greg S Lee; Mark E Davis; Saleh Elomari; Ronald C Medrud, A.; S I Zones. *J. Am. Chem. Soc.* **1999**, *122*, 263–273.
- (47) Leonowicz, M. E.; Lawton, J. A.; Lawton, S. L.; Rubin, M. K. *Science* **1994**, *264*, 1910–1913.
- (48) Zhou, D.; Bao, Y.; Yang, M.; He, N.; Yang, G. *J. Mol. Catal. A Chem.* **2006**, *244*, 11–19.
- (49) Li, Y.; Guo, W.; Fan, W.; Yuan, S.; Li, J.; Wang, J.; Jiao, H.; Tatsumi, T. *J. Mol. Catal. A Chem.* **2011**, *338*, 24–32.
- (50) Bučko, T.; Hafner, J. *J. Catal.* **2015**, *329*, 32–48.
- (51) Li, Y.-P.; Gomes, J.; Mallikarjun Sharada, S.; Bell, A. T.; Head-Gordon, M. *J. Phys. Chem. C* **2015**, *119*, 1840–1850.
- (52) Shao, Y.; Molnar, L. F.; Jung, Y.; Kussmann, J.; Ochsenfeld, C.; Brown, S. T.; Gilbert, A. T. B.; Slipchenko, L. V.; Levchenko, S. V.; O'Neill, D. P.; DiStasio, R. A., Jr; Lochan, R. C.; Wang, T.; Beran, G. J. O.; Besley, N. A.; Herbert, J. M.; Lin, C. Y.; Van Voorhis, T.; Chien, S. H.; Sodt, A.; Steele, R. P.; Rassolov, V. A.; Maslen, P. E.; Korambath, P. P.; Adamson, R. D.; Austin, B.; Baker, J.; Byrd, E. F. C.; Dachsel, H.; Doerksen, R. J.; Dreuw, A.; Dunietz, B. D.; Dutoi, A. D.; Furlani, T. R.; Gwaltney, S. R.; Heyden, A.; Hirata, S.; Hsu, C.-P.; Kedziora, G.; Khalliulin, R. Z.; Klunzinger, P.;

- 1
2
3 Lee, A. M.; Lee, M. S.; Liang, W.; Lotan, I.; Nair, N.; Peters, B.; Proynov, E. I.;
4 Pieniazek, P. A.; Rhee, Y. M.; Ritchie, J.; Rosta, E.; Sherrill, C. D.; Simmonett, A. C.;
5 Subotnik, J. E.; Woodcock, H. L., III; Zhang, W.; Bell, A. T.; Chakraborty, A. K.;
6 Chipman, D. M.; Keil, F. J.; Warshel, A.; Hehre, W. J.; Schaefer, H. F., III; Kong, J.;
7 Krylov, A. I.; Gill, P. M. W.; Head-Gordon, M. *Phys. Chem. Chem. Phys.* **2006**, *8*,
8 3172–3191.
9
10 (53) Verstraelen, T.; Van Speybroeck, V.; Waroquier, M. *J. Chem. Inf. Model.* **2008**, *48*,
11 1530–1541.
12 (54) Chai, J.-D.; Head-Gordon, M. *J. Chem. Phys.* **2008**, *128*, 084106.
13 (55) Chai, J.-D.; Head-Gordon, M. *Phys. Chem. Chem. Phys.* **2008**, *10*, 6615–6620.
14 (56) Foloppe, N.; MacKerell, A. D., Jr. *J. Comput. Chem.* **2000**, *21*, 86–104.
15 (57) Yin, D.; MacKerell, A. D. *J. Comput. Chem.* **1998**, *19*, 334–348.
16 (58) Vanommeslaeghe, K.; Hatcher, E.; Acharya, C.; Kundu, S.; Zhong, S.; Shim, J.; Darian,
17 E.; Guvench, O.; Lopes, P.; Vorobyov, I.; Mackerell, A. D. *J. Comput. Chem.* **2010**, *31*,
18 671–690.
19 (59) Behn, A.; Zimmerman, P. M.; Bell, A. T.; Head-Gordon, M. *J. Chem. Phys.* **2011**, *135*,
20 224108.
21 (60) Baker, J. *J. Comput. Chem.* **1986**, *7*, 385–395.
22 (61) De Moor, B. A.; Reyniers, M.-F.; Marin, G. B. *Phys. Chem. Chem. Phys.* **2009**, *11*,
23 2939–22.
24 (62) De Moor, B. A.; Reyniers, M.-F.; Gobin, O. C.; Lercher, J. A.; Marin, G. B. *J. Phys.*
25 *Chem. C* **2011**, *115*, 1204–1219.
26 (63) De Moor, B. A.; Ghysels, A.; Reyniers, M.-F.; Van Speybroeck, V.; Waroquier, M.;
27 Marin, G. B. *J. Chem. Theory Comput.* **2011**, *7*, 1090–1101.
28 (64) Ghysels, A.; Van Neck, D.; Van Speybroeck, V.; Verstraelen, T.; Waroquier, M. *J.*
29 *Chem. Phys.* **2007**, *126*, 224102.
30 (65) Ghysels, A.; Verstraelen, T.; Hemelsoet, K.; Waroquier, M.; Van Speybroeck, V. *J.*
31 *Chem. Inf. Model.* **2010**, *50*, 1736–1750.
32 (66) Janda, A.; Vlaisavljevich, B.; Smit, B.; Lin, L.-C.; Bell, A. T. *J. Phys. Chem. C* **2017**,
33 *121*, 1618–1638.
34 (67) Gomes, J.; Head-Gordon, M.; Bell, A. T. *J. Phys. Chem. C* **2014**, *118*, 21409–21419.
35 (68) Laio, A.; Parrinello, M. *Proc. Nat. Acad. Sci.* **2002**, *99*, 12562–12566.
36 (69) Ensing, B.; Laio, A.; Parrinello, M.; Klein, M. L. *J. Phys. Chem. B* **2005**, *109*, 6676–
37 6687.
38 (70) Dellago, C.; Bolhuis, P. G.; Geissler, P. L. *Transition Path Sampling*; John Wiley &
39 Sons, Inc.: Hoboken, NJ, USA, 2002; Vol. 123, pp 1–78.
40 (71) Bolhuis, P. G.; Chandler, D.; Dellago, C.; Geissler, P. L. *Annu. Rev. Phys. Chem.* **2002**,
41 *53*, 291–318.
42 (72) Moors, S. L. C.; De Wispelaere, K.; Van der Mynsbrugge, J.; Waroquier, M.; Van
43 Speybroeck, V. *ACS Catal.* **2013**, *3*, 2556–2567.
44 (73) Van der Mynsbrugge, J.; Moors, S. L. C.; De Wispelaere, K.; Van Speybroeck, V.
45 *ChemCatChem* **2014**, *6*, 1906–1918.
46 (74) De Wispelaere, K.; Ensing, B.; Ghysels, A.; Meijer, E. J.; Van Speybroeck, V. *Chem.*
47 *Eur. J.* **2015**, *21*, 9385–9396.
48 (75) Van Speybroeck, V.; De Wispelaere, K.; Van der Mynsbrugge, J.; Vandichel, M.;
49 Hemelsoet, K.; Waroquier, M. *Chem. Soc. Rev.* **2014**, *43*, 7326–7357.
50
51
52
53
54
55
56
57
58
59
60

- 1
2
3 (76) Van Speybroeck, V.; Hemelsoet, K.; Joos, L.; Waroquier, M.; Bell, R. G.; Catlow, C. R.
4 *A. Chem. Soc. Rev.* **2015**, *44*, 7044–7111.
5 (77) Hajek, J.; Van der Mynsbrugge, J.; De Wispelaere, K.; Cnudde, P.; Vanduyfhuys, L.;
6 Waroquier, M.; Van Speybroeck, V. *J. Catal.* **2016**, *340*, 227–235.
7 (78) Cnudde, P.; De Wispelaere, K.; Van der Mynsbrugge, J.; Waroquier, M.; Van
8 Speybroeck, V. *J. Catal.* **2017**, *345*, 53–69.
9 (79) Ohio Supercomputer Center, <http://osc.edu/ark:/19495/f5s1ph73>, 1987.
10
11
12
13
14
15
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